Nonperturbative propagators and vertices from Dyson-Schwinger equations



Markus Q. Huber

arXiv:1808.05227
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Excited QCD 2019 Schladming, Austria February 2, 2019

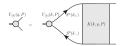




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Hadronic bound states

Bound state equations: E.g., meson



Ingredients:

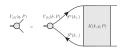
Interaction kernel K

Quark propagator S

$$\longrightarrow S(p) \qquad -1 \qquad = \qquad \longrightarrow -1 \qquad + \qquad \searrow \Gamma_{\mu}(p, q)$$

Hadronic bound states

Bound state equations: E.g., meson



Ingredients:

 \bullet Interaction kernel K

Quark propagator S

$$\sum_{S(p)}^{-1} = \sum_{S_0(p)}^{-1} + \gamma_{\mu} \sum_{S(q)}^{D_{\mu\nu}(p-q)} \Gamma_{\mu}(p,q)$$

Approaches:

Phenomenological (bottom-up):
 Model interactions

- From first principles (top-down):
 Piecing together the elementary
 pieces
- → Talks by Adrien, Miramóntes, Wallbott

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Bottom-up vs. top-down

Bottom-up:

- Modeling to describe certain quantities, symmetries as guiding principles
- Example: Rainbow-ladder truncation with Maris-Tandy interaction:
 - 1 function, 2 parameters $G(k^2)$
 - \rightarrow Good description of, e.g., pseudoscalars

Top-down:

Parameters of QCD only

 9 dressings for gluon propagator and quark-gluon vertex:

$$D(k^2), \Gamma_i^{A\bar{q}q}(p,q,r), i = 1,...,8$$

- \rightarrow Technically complex
- Maximal flexibility ↔ consistency not easy to achieve

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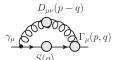
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In the past

Mostly bottom-up (hadron pheno) and top-down with bottom-up admixtures

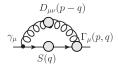
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Introduction



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Extending truncations



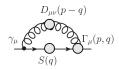
Bottom-up:

Introduction

Effective interaction via $g^2 D_{\mu\nu}(p) \Gamma_{\mu}(p,q) o Z_2 \widetilde{Z}_3 D^{(0)}_{\mu\nu}(p) \gamma_{\mu} \mathcal{G}((p+q)^2)$

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The elementary pieces



Bottom-up:

Effective interaction via $g^2 D_{\mu\nu}(p) \Gamma_{\mu}(p,q) \rightarrow Z_2 \widetilde{Z}_3 D_{\mu\nu}^{(0)}(p) \gamma_{\mu} \mathcal{G}((p+q)^2)$

Top-down:

Gluon propagator
$$D_{\mu\nu}(p^2)$$
: $-\frac{1}{2}$ $-\frac{1}{2}$

Quark-gluon vertex $\Gamma_{\mu}(p,q)$:

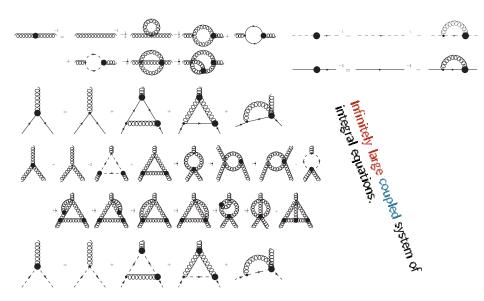


ightarrow Couple to infinity of equations.

 \rightarrow Gluonic part is crucial. \Rightarrow Understand pure QCD (Yang-Mills theory) first.

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Introduction



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• Influence of higher correlation functions?

qualitative? quantitative? negligible?

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qualitative? quantitative? negligible?

Hierarchy of diagrams/correlation functions?
 negligible diagrams? irrelevant correlation functions for specific questions?

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- conflicting requirements for models? parameter-free solution?

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- Influence of higher correlation functions?
- qualitative? quantitative? negligible?
- Hierarchy of diagrams/correlation functions? negligible diagrams? irrelevant correlation functions for specific questions?
- Model dependence → Self-contained truncation? conflicting requirements for models? parameter-free solution?
- How to realize resummation?

higher loop contributions?

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higher loop contributions?

Systematics and tests?

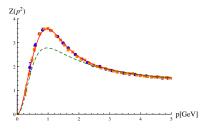
comparison to other methods, self-tests?

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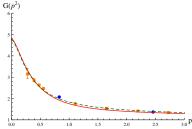
Example of a bottom-up calculation

Extending truncations

Propagators and ghost-gluon vertex with three-gluon vertex model: One-loop truncation of gluon propagator with an optimized effective model (contains zero crossing) [MQH, von Smekal '13; lattice: Sternbeck '06]:



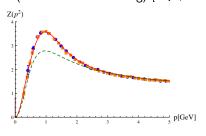
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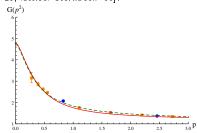


Good quantitative agreement for ghost and gluon dressings.

Markus Q. Huber Giessen University February 2, 2019 7/29 Propagators and ghost-gluon vertex with three-gluon vertex model:

One-loop truncation of gluon propagator with an optimized effective model
(contains zero crossing) [MQH, von Smekal '13; lattice: Sternbeck '06]:





Good quantitative agreement for ghost and gluon dressings.

QCD is only this:

$$\begin{split} & \mathcal{L} = -\frac{1}{2} \operatorname{Tr} \left(\operatorname{F}_{\mu\nu} \operatorname{F}^{\mu\nu} \right) + \sum_{j} \overline{\varphi}_{j} [i \, \gamma^{\mu} \operatorname{D}_{\mu} - m_{j}] \varphi_{j} \\ & \text{MOBEI} \quad \operatorname{F}_{\mu\nu} = \partial_{\mu} \operatorname{A}_{\nu} - \partial_{\nu} \operatorname{A}_{\mu} + i g \left[\operatorname{A}_{\mu} \operatorname{A}_{\nu} \right] \end{split}$$

UND D. = 2. + igA.

Can we do with only that?

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A lesson from three dimensions?

Three-dimensional Yang-Mills theory is finite.

- → No renormalization
- \rightarrow Leading pertubative contributions $\propto g^2/p$

⇒ Testbed for functional calculations.

Various methods employed:

- Lattice: [Bornyakov, Cucchieri, Maas, Mendes, Mitriushkin, Rogalyov, ...]
- Coupled propagator DSEs: [Maas, Wambach, Grüter, Alkofer '04]
- (R)GZ: [Dudal, Gracey, Sorella, Vandersickel, Verschelde '08]
- DSEs of PT-BFM: [Aguilar, Binosi, Papavassiliou '10]
- YM + mass term: [Tissier, Wschebor '10, '11]
- FRG: [Corell, Cyrol, Mitter, Pawlowski, Strodthoff '18]

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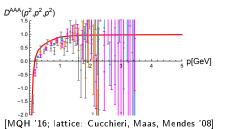
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Study effect of individual diagrams...

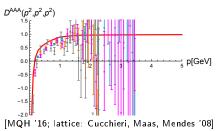
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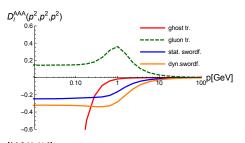
Cancellations in three-gluon vertex



- Close to tree-level above 1 GeV
- Good agreement with lattice data.
 Linear IR divergence [Pelaez, Tissier,
- Wschebor '13; Aguilar et al. '13]
- Similar results from FRG [Corell et al. '18]

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- Individual contributions large.
- Sum is small!

[MQH '16]

Introduction

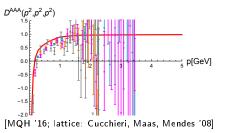
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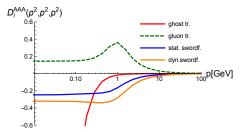
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Cancellations in three-gluon vertex



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- Individual contributions large.
- Sum is small!

 \rightarrow In four dimensions similar qualitative effects, but renormalization complicates things.

[MQH '16]

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Resummed one-loop order: anomalous dimension $\gamma = -13/22$

$$\left(1 + \frac{\alpha(s)11N_c}{12\pi} \ln \frac{p^2}{s}\right)^{\gamma}$$

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Introduction

A question of consistency? The UV behavior of the gluon propagator

Resummed one-loop order: anomalous dimension $\gamma = -13/22$

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One-loop anomalous dimension

Origin in resummation of higher order diagrams.

However, one-loop truncation discards some terms.



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One-loop anomalous dimension

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However, one-loop truncation discards some terms.



→ Puts constraints on UV behavior of vertices if one wants a self-consistent solution [von Smekal, Hauck, Alkofer '97].

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Fixing the UV behavior of the gluon propagator I

First possibility:

Modify the UV behavior of the integrand, e.g., replace the renormalization constant by a momentum dependent function [von Smekal, Hauck, Alkofer '97] ('RG improvement'), adapt employed models.

$$\widetilde{Z}_1 \to f(p^2)$$

Part of the modeling.

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Examples:

- Yang-Mills propagators, e.g., [von Smekal, Hauck, Alkofer '97; Fischer, Alkofer '02;
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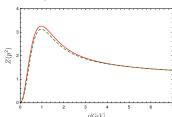
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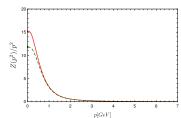
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IR completion has an effect on the gluon propagator [MQH, von Smekal '14]:





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Second possibility:

Include higher perturbative terms.

Worked out analytically for ϕ^3 -theory [MQH $^{\prime}$ 18].

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Fixing the UV behavior of the gluon propagator II

Extending truncations

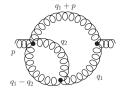
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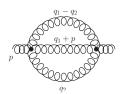
Introduction

Include higher perturbative terms.

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 \rightarrow Two-loop diagrams





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Fixing the UV behavior of the gluon propagator II

Extending truncations

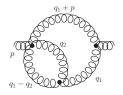
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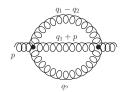
Introduction

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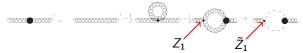
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 \rightarrow Two-loop diagrams





→ Contributions also from renormalization constants in front of one-loop diagrams.



⇒ All two-loop contributions in the gluon propagator are included. And higher contributions...

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Resummed behavior

Minimal requirements to obtain one-loop resummed behavior:

- Squint diagram (sunset has no $g^4 \ln^2 p^2$)
- Correct anomalous dimensions of three-point functions
- Correct renormalization (constants)

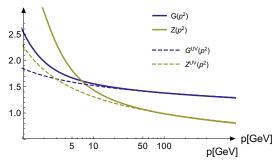
Markus Q. Huber Giessen University February 2, 2019 13/29 Introduction

Extending truncations

Resummed behavior

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- Correct renormalization (constants)



Resummed behavior is recovered [MQH '17].

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Extending truncations

Extending truncations

Various ways to extend truncations.

Extension of the previous one:

Introduction

- Vertex tensors beyond tree-level tensor
- Include neglected diagrams
- Include neglected correlation functions

Extensions also test the previous truncations!

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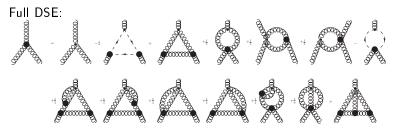
Three-gluon vertex DSE

[Cucchieri, Maas, Mendes '08; Alkofer, MQH, Schwenzer '09; Pelaez, Tissier, Wschebor '13; Aguilar et al. '13; Blum, et al. '14; Eichmann, Alkofer, Vujinovic '14; Cyrol et al. '16; Williams, Fischer, Heupel '16; Sternbeck '16; Athenodorou et al. 16; Duarte et al. '16; Boucaud et al. '17]

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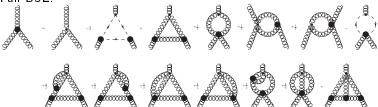


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Full DSE:



Perturbative one-loop truncation [Blum, MQH, Mitter von Smekal '14; Eichmann, Alkofer, Vujinovic '14; Williams, Fischer, Heupel '16]:

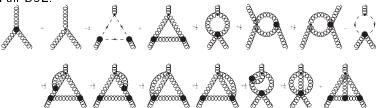


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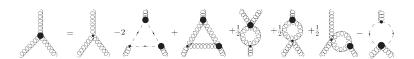
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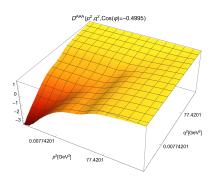
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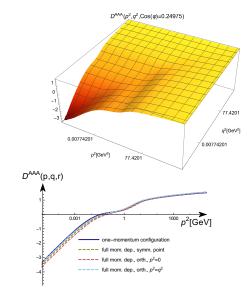


Non-perturbative one-loop truncation [MQH '17]:





- Kinematic dependence weak.
- In the following: One-momentum configuration approximation



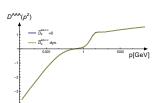
Influence of two-ghost-two-gluon vertex



Influence of two-ghost-two-gluon vertex



Coupled system of ghost-gluon, three-gluon and four-gluon vertices with and without two-ghost-two-gluon vertex [MQH '17]:



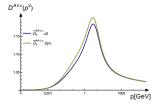
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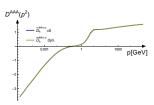


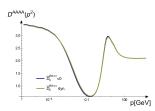




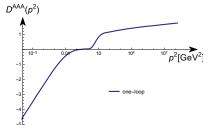
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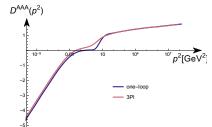


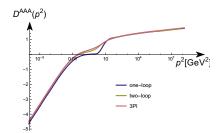


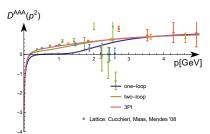


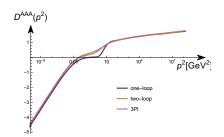
- Small influence on ghost-gluon vertex (< 1.7%)
- Negligible influence on three- and four-gluon vertices.



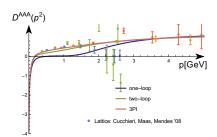


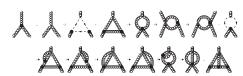


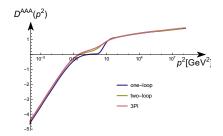


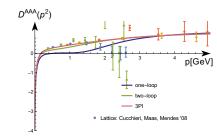


- Two-loop truncation: All diagrams except the one with a five-point function.
- One-momentum configuration approximation.

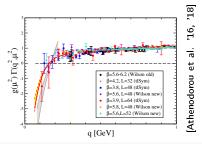








- Difference between two-loop DSE and 3PI smaller than lattice error.
- Zero crossing in agreement with other approaches, e.g., [Pelaez et al. '13; Aguilar et al. '13; Cyrol et al. '15; Athenodorou et al. '16; Duarte et al. '16; Sternbeck et al. '17]



The two-ghost-two-gluon vertex

Non-primitively divergent correlation function \rightarrow No guide from tree-level tensor. \rightarrow Use full basis.

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Two-ghost-two-gluon vertex



$$\Gamma^{AA\bar{c}c,abcd}_{\mu\nu}(p,q;r,s) = \mathbf{g^4} \sum_{k=1}^{40} \rho^{k,abcd}_{\mu\nu} D^{AA\bar{c}c}_{k(i,j)}(p,q;r,s)$$

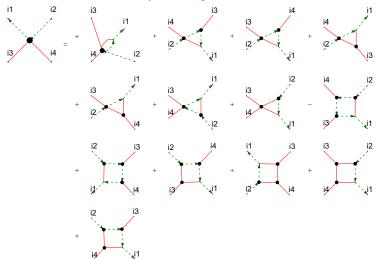
with

$$\rho_{\mu\nu}^{k,abcd} = \sigma_i^{abcd} \tau_{\mu\nu}^j, \qquad k = k(i,j) = 5(i-1) + j$$

Introduction

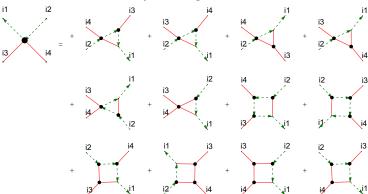
The two-ghost-two-gluon vertex DSE

2 DSEs, choose the one with the ghost leg attached to the bare vertex → Truncation discards only one diagram.



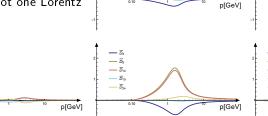
The two-ghost-two-gluon vertex DSE

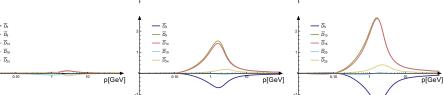
2 DSEs, choose the one with the ghost leg attached to the bare vertex → Truncation discards only one diagram.



Kinematic approximation: one-momentum configuration

- Dimensionless dressing functions \overline{D}_k .
- Each plot one Lorentz tensor.





→ Two classes of dressings: 13 very small, 12 not small

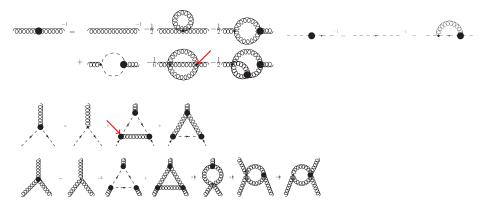
 \rightarrow No nonzero solution for $\{\sigma_6, \sigma_7, \sigma_8\}$ found.

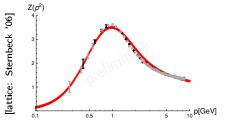
[MQH '17]

p[GeV

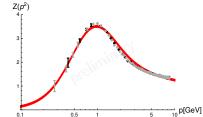
3PI system of primitively divergent correlation functions

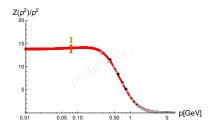
Three-loop expansion of 3PI effective action [Berges '04]:

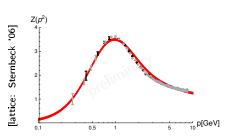




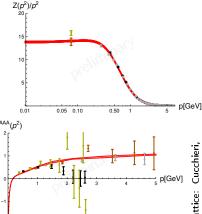
Results for fully coupled 3PI system







- Details of renormalization crucial!
- Other details also important.
- Very small angle dependence of three-gluon vertex.
- Slight bending down of gluon propagator in IR.



[lattice: Cucchieri Maas Mendes 708

Open checks

- Effects of larger tensor bases, in particular of the three-gluon vertex
- Renormalization

What tests can be done?

Couplings

Couplings can be defined from every vertex, e.g., [Allés et al. '96; Alkofer et al., '05; Eichmann et al. '14]:

$$\alpha_{ghg}(p^2) = \alpha(\mu^2) (D^{A\bar{c}c}(p^2))^2 G^2(p^2) Z(p^2),$$

$$\alpha_{3g}(p^2) = \alpha(\mu^2) (C^{AAA}(p^2))^2 Z^3(p^2),$$

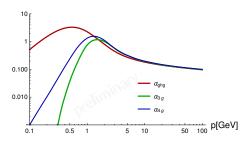
$$\alpha_{4g}(p^2) = \alpha(\mu^2) F^{AAAA}(p^2) Z^2(p^2).$$

They must agree perturbatively (STIs). This agreement is important also in coupled systems of functional equations and constitutes a highly non-trivial check of a truncation [Mitter, Pawlowski, Strodthoff '14].

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$$\begin{split} &\alpha_{\mathsf{ghg}}(p^2) = \alpha(\mu^2) \left(D^{A\bar{c}c}(p^2) \right)^2 G^2(p^2) Z(p^2), \\ &\alpha_{\mathsf{3g}}(p^2) = \alpha(\mu^2) \left(C^{AAA}(p^2) \right)^2 Z^3(p^2), \\ &\alpha_{\mathsf{4g}}(p^2) = \alpha(\mu^2) F^{AAAA}(p^2) Z^2(p^2). \end{split}$$

They must agree perturbatively (STIs). This agreement is important also in coupled systems of functional equations and constitutes a highly non-trivial check of a truncation [Mitter, Pawlowski, Strodthoff '14].



Ghost-gluon vs. other couplings: Further checks required.

Renormalization with a hard UV cutoff

Introduces quadratic divergences.

Note: Appears already perturbatively!

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Note: Appears already perturbatively!

The breaking of gauge covariance by the UV regularization leads to spurious (quadratic) divergences.

Due to the anomalous running, this behaves as (at one-loop resummed level)

$$\frac{\Lambda_{\mathrm{QCD}}^2}{p^2}(-1)^{2\delta}\Gamma(1+2\delta,-\ln(\Lambda^2/\Lambda_{\mathrm{QCD}}^2))$$

Many ways to deal with them, e.g., Brown-Pennington projector, modifications of integrands/vertices, fitting, seagull identities, ... [MQH, von Smekal '14].

Examples for renormalization with a hard UV cutoff

Here: Second renormalization condition

Breaking of gauge covariance → mass counter term [Collins '84]

Renormalization condition: D(0) = c [Meyers, Swanson '14]

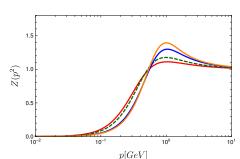
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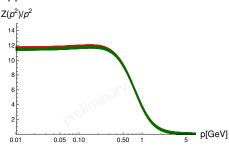
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Extreme example: One-loop truncation with bare vertices in three dimensions. [MQH '16].

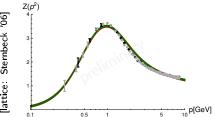


Better example: Full system with one-momentum configuration approximation.



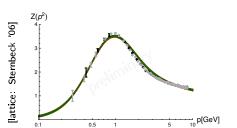
Results for fully coupled 3PI system revisited

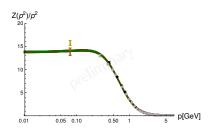
Vary the renormalization condition D(0):



Results for fully coupled 3PI system revisited

Vary the renormalization condition D(0):





- \rightarrow Two solutions on top of each other. D(0) is not a parameter of the system.
- → Provides a self-test of a truncation.

Summary and conclusions

Towards a systematic understanding of truncations of functional equations to access their full potential.

Introduction

Extending truncations

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Infinite set of equations with no evident hierarchy...Is there hope?

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- Add quarks
- Finite temperature

- Bound states
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Four-gluon vertex

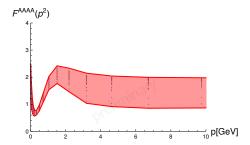
Four-point functions have 6 kinematic variables.

Organize via S4 permutation group [Eichmann, Fischer, Heupel '15] and restrict to singlet and doublet. \rightarrow Three variables.

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Deviations from leading perturbative behavior small, but larger angle dependence than three-gluon vertex.

Kinematic approximation: one-momentum configuration

Four-ghost vertex

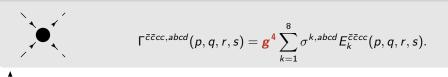


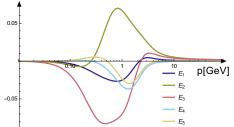
$$\Gamma^{\bar{c}\bar{c}cc,abcd}(p,q,r,s) = \mathbf{g}^4 \sum_{k=1}^8 \sigma^{k,abcd} E_k^{\bar{c}\bar{c}cc}(p,q,r,s).$$

Results for the four-ghost vertex

Kinematic approximation: one-momentum configuration

Four-ghost vertex





 \rightarrow All dressings very small.

[MQH '17]